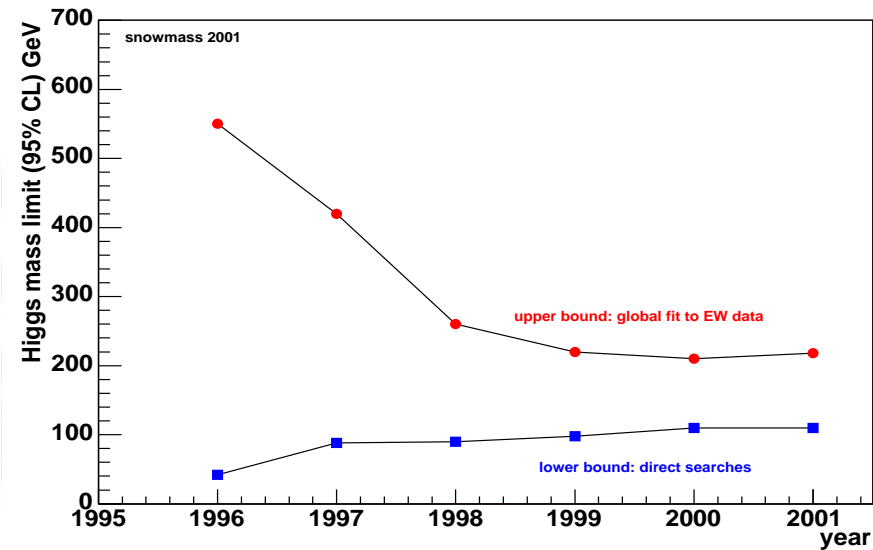
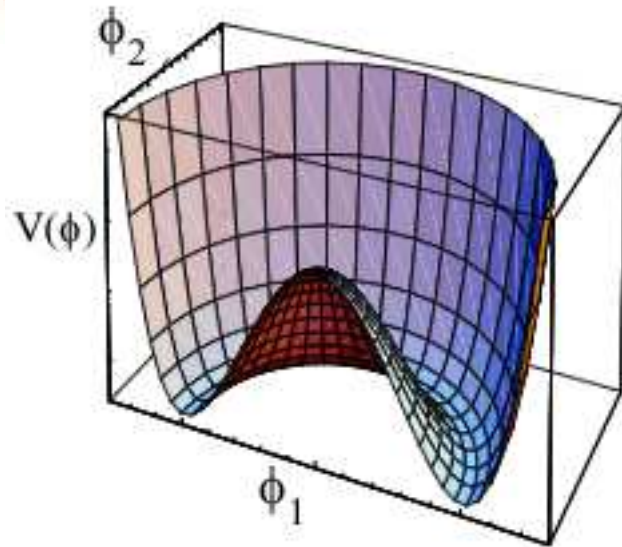




$W_L W_L$ scattering at LHC: An approach to the Theoretical Background

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- Standard Model: A very good model satisfying theorists and experimentalists.
- It explains the **Electroweak Symmetry Breaking-EWSB** by introducing the **Higgs** boson.



- However, any assumptions and any mass limits are **model dependent**.
- Alternative models to explain EWSB: SM with heavy higgs, technicolor, composite models etc etc
- Enhanced production of **longitudinal** vector boson pairs is one of the most characteristic signals of the new physics

- Describes the low energy effects of different strongly interacting models of the Symmetry Breaking Sector.
- The differences among underlying theories appear through the values of the effective chiral couplings.
- It includes operators up to order of $s^2 (E^4)$.
- At the lowest order:

$$\mathcal{L}^{(2)} = \frac{u^2}{4} \text{Tr}\{D_\mu U D^\mu U^\dagger\} \quad (1)$$

where

$$D_\mu U = d_\mu U - W_\mu U + U B_\mu$$

$$W_\mu = -ig \frac{\sigma^\alpha W_\mu^\alpha}{2} \quad B_\mu = ig \frac{\sigma^3 B_\mu}{2} \quad U = \exp\left(\frac{i\omega^\alpha \sigma^\alpha}{u}\right)$$

where σ are the Pauli matrices, ω are the three Goldstone bosons and $u = 246$ GeV

- The next term includes the model-dependent effective couplings:

$$\mathcal{L}^{(4)} = \alpha_4 \left(\text{Tr}\{D_\mu U D^\mu U^\dagger\}\right)^2 + \alpha_5 \left(\text{Tr}\{D_\mu U D^\nu U^\dagger\}\right)^2 \quad (2)$$

- The α_4 and α_5 depend on the model but also on the renormalization scale μ . With $\mu = 1$ TeV we expect them to be in the range of $[-0.01, 0.01]$
- Additional terms of the order of s^2 contribute to anomalous trilinear couplings between vector bosons.

- For the $W_L^a W_L^b \rightarrow W_L^c W_L^d$ in the weak isospin space:

$$\mathcal{M}(W_L^a W_L^b \rightarrow W_L^c W_L^d) \equiv A(s, t, u) \delta^{ab} \delta^{cd} + A(t, s, u) \delta^{ac} \delta^{bd} + A(u, t, s) \delta^{ad} \delta^{bc} \quad (3)$$

where the key amplitude $A(s, t, u)$ is:

$$A(s, t, u) = \frac{s}{u^2} + \frac{1}{4\pi u^4} (2\alpha_5 s^2 + \alpha_4 (t^2 + u^2)) + \frac{1}{16\pi^2 u^4} \left(-\frac{t}{6} (s + 2t) \log \left(-\frac{t}{\mu^2} \right) - \frac{u}{6} (s + 2u) \log \left(-\frac{u}{\mu^2} \right) - \frac{s^2}{2} \log \left(-\frac{s}{\mu^2} \right) \right) \quad (4)$$

(In the above: W_L denotes either W_L^\pm or Z_L , $W_L^\pm = \frac{W_L^1 \mp i W_L^2}{\sqrt{2}}$, $Z_L = W_L^3$, $a, b, c, d = 1, 2, 3, 4$ and s, t, u are the Mandelstam kinematical variables.)

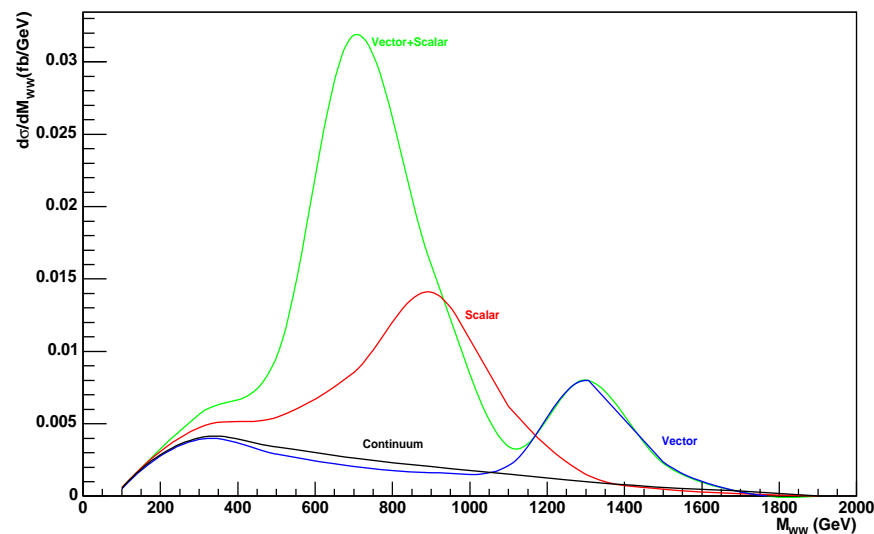
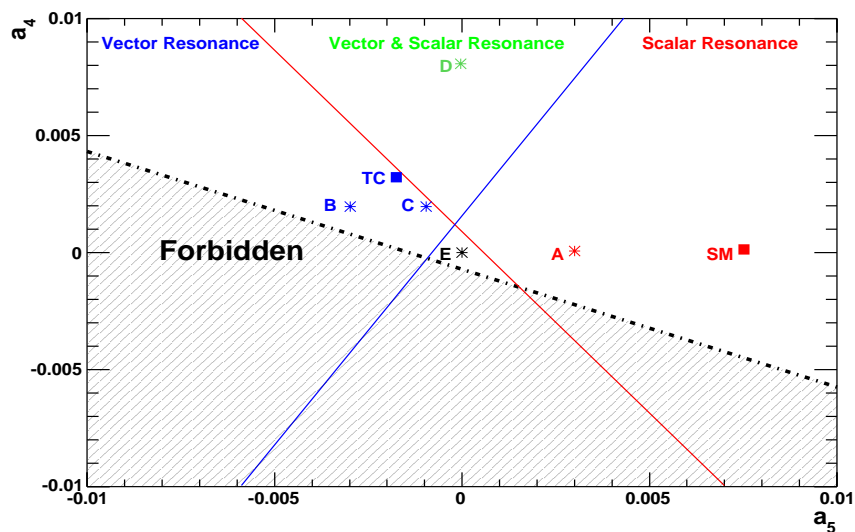
- Precise measurement of the $W_L W_L \rightarrow W_L W_L$ scattering cross-section would allow the extraction of the α_4 and α_5 parameters.

- The usual EWChL approach doesn't respect **unitarity**.
- Unitarity is restored by applying different **unitarization protocols**, for example: **Inverse Amplitude Method (Pade)**, N/D protocol etc.
- The **position** and the **nature** of the resonances **depend strongly** upon the unitarisation procedure.
(see for example Phys.Rev.D **65** 096014 for comparison between the Pade and the N/D protocols)
- Using the Pade protocol, we obtain the following mass and the width of the resonances:

$$M_V^2 = \frac{u^2}{4(\alpha_4 - 2\alpha_5) + \frac{1}{144\pi^2}}, \quad \Gamma_V = \frac{M_V^3}{96\pi u^2} \quad (5)$$

$$M_S^2 = \frac{12u^2}{16(11\alpha_5 + 7\alpha_4) + \frac{101}{48\pi^2}}, \quad \Gamma_S = \frac{M_S^3}{16\pi u^2} \quad (6)$$

- For equal masses, scalar resonances would be **6 times wider** than vector resonances.



Scenario	α_4	α_5	Resonance Mass (GeV)
Scalar(A)	0.0	0.003	989.8
Vector(B)	0.002	-0.003	1360.3
Scalar + Vector (D)	0.008	0.0	809.6 + 1360.3
Continuum (E)	0.0	0.0	NA

- PYTHIA has been modified to include the EWChL and to produce the resonances for different parameters according to the Pade protocol.
- Forbidden region: Where causality is violated, i.e. $\frac{32}{3}(\alpha_5 + 2\alpha_4) + \frac{273}{864\pi^2} < 0$